

FIG. 1 is a schematic diagram of a network topology. The network is divided into four areas: Area 0.0.0.1, Area 0.0.0.2, Area 0.0.0.0, and Area 0.0.0.3. Area 0.0.0.1 contains nodes 111 and 121. Area 0.0.0.2 contains nodes 112 and 122. Area 0.0.0.0 contains nodes 113, 114, 115, 116, 117, 118, 119, 123, 124, 125, and 126. Area 0.0.0.3 contains nodes 127 and 128. The nodes are interconnected by links with associated numerical values. The connections are as follows: 111 is connected to 121 (value 100). 112 is connected to 122 (value 100). 113 is connected to 114 (value 200) and 115 (value 100). 114 is connected to 116 (value 100). 115 is connected to 117 (value 50). 116 is connected to 118 (value 200). 117 is connected to 119 (value 1000). 118 is connected to 123 (value 50). 119 is connected to 127 (value 200). 123 is connected to 124 (value 100). 124 is connected to 125 (value 100). 125 is connected to 126 (value 100). 126 is connected to 127 (value 100). 127 is connected to 128 (value 100). The network is also divided into four areas: Area 0.0.0.1, Area 0.0.0.2, Area 0.0.0.0, and Area 0.0.0.3. Area 0.0.0.1 contains nodes 111 and 121. Area 0.0.0.2 contains nodes 112 and 122. Area 0.0.0.0 contains nodes 113, 114, 115, 116, 117, 118, 119, 123, 124, 125, and 126. Area 0.0.0.3 contains nodes 127 and 128. The nodes are interconnected by links with associated numerical values. The connections are as follows: 111 is connected to 121 (value 100). 112 is connected to 122 (value 100). 113 is connected to 114 (value 200) and 115 (value 100). 114 is connected to 116 (value 100). 115 is connected to 117 (value 50). 116 is connected to 118 (value 200). 117 is connected to 119 (value 1000). 118 is connected to 123 (value 50). 119 is connected to 127 (value 200). 123 is connected to 124 (value 100). 124 is connected to 125 (value 100). 125 is connected to 126 (value 100). 126 is connected to 127 (value 100). 127 is connected to 128 (value 100).

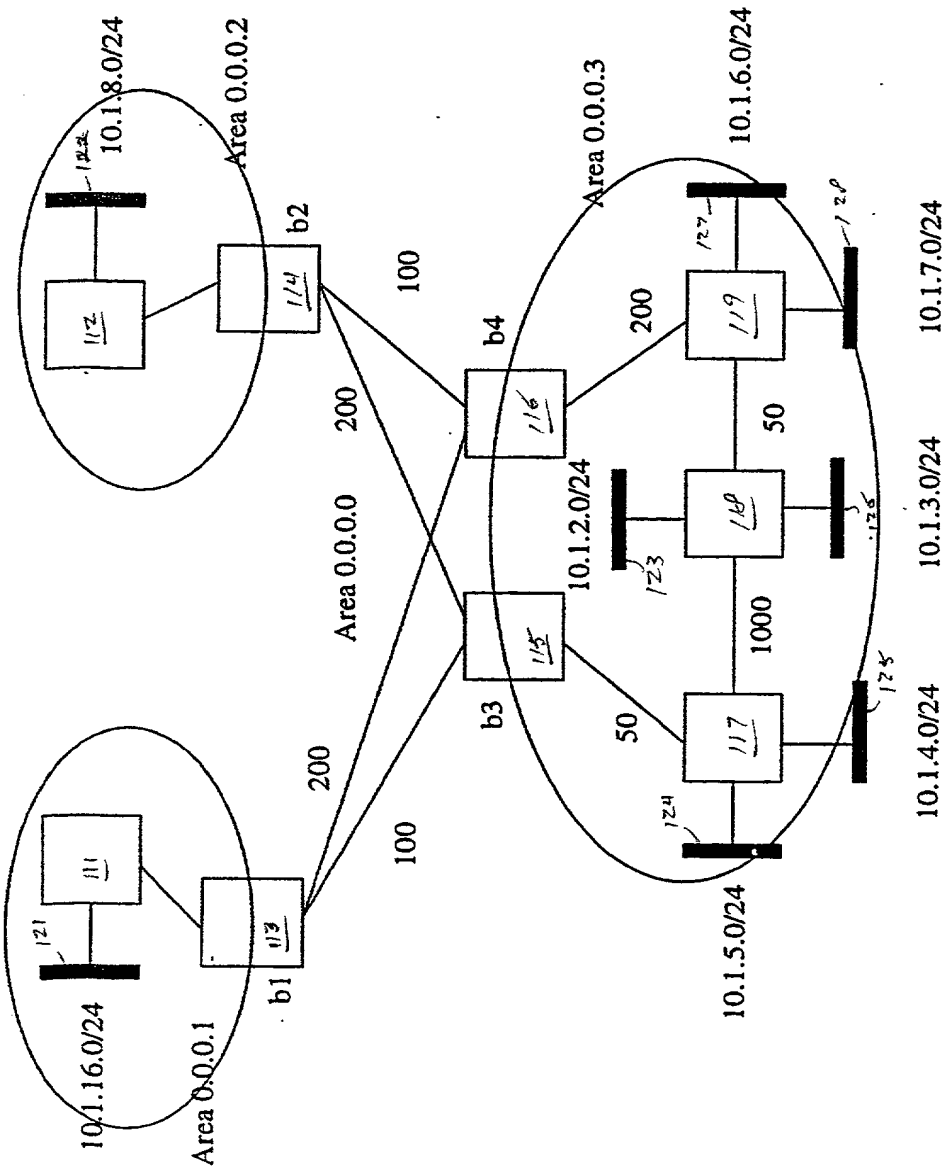


FIGURE 1

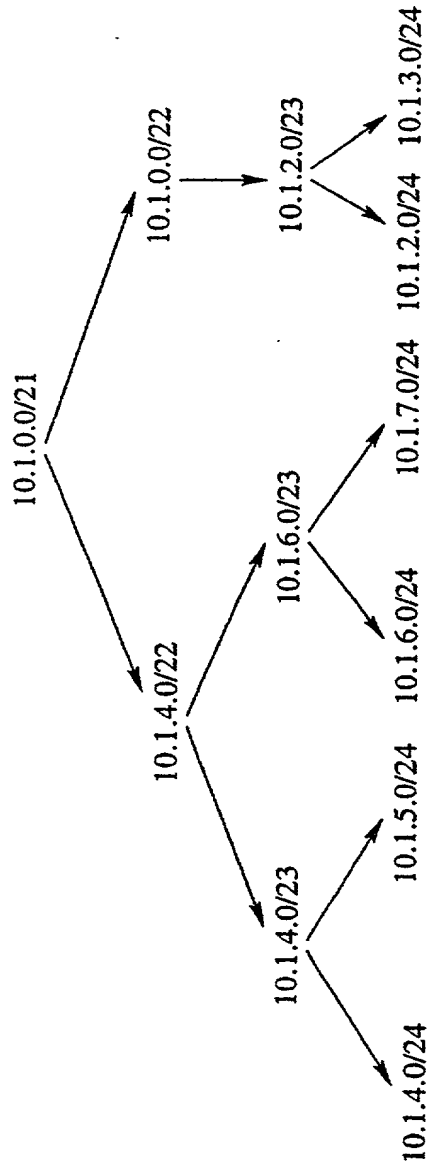


FIGURE 2

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procedure COMPUTEMINERROR(Aggregate  $x$ , Aggregate  $y$ , integer  $l$ )
1. if subTree[ $x$ ,  $y$ ,  $l$ ].computed = true
2.   return [subTree[ $x$ ,  $y$ ,  $l$ ].error, subTree[ $x$ ,  $y$ ,  $l$ ].aggregates]
3. minError := minError1 := minError2 :=  $\infty$ 
4. if  $x$  is a leaf {
5.   minError1 :=  $\sum_{s \in S} D(s, t) * (lsp(s, x, \{y\}, W_A) - lsp(s, x))$ 
6.   if  $l > 0$ 
7.     minError2 :=  $\sum_{s \in S} D(s, t) * (lsp(s, x, \{x\}, W_A) - lsp(s, x))$ 
8.   if minError1  $\leq$  minError2
9.     [subTree[ $x$ ,  $y$ ,  $l$ ].error, subTree[ $x$ ,  $y$ ,  $l$ ].aggregates] := [minError1,  $\emptyset$ ]
10.  else
11.    [subTree[ $x$ ,  $y$ ,  $l$ ].error, subTree[ $x$ ,  $y$ ,  $l$ ].aggregates] := [minError2,  $\{x\}$ ]
12. }
13. if  $x$  has a single child  $u$  {
14.   [minError1, aggregates1] := COMPUTEMINERROR( $u$ ,  $y$ ,  $l$ )
15.   if  $l > 0$ 
16.     [minError2, aggregates2] := COMPUTEMINERROR( $u$ ,  $x$ ,  $l - 1$ )
17.   if minError1  $\leq$  minError2
18.     [subTree[ $x$ ,  $y$ ,  $l$ ].error, subTree[ $x$ ,  $y$ ,  $l$ ].aggregates] := [minError1, aggregates1]
19.   else
20.     [subTree[ $x$ ,  $y$ ,  $l$ ].error, subTree[ $x$ ,  $y$ ,  $l$ ].aggregates] := [minError2, aggregates2  $\cup \{x\}$ ]
21. }
22. if  $x$  has children  $u$  and  $v$  {
23.   for  $i := 0$  to  $l$  {
24.     [minError1, aggregates1] := COMPUTEMINERROR( $u$ ,  $y$ ,  $i$ )
25.     [minError2, aggregates2] := COMPUTEMINERROR( $v$ ,  $y$ ,  $k - i$ )
26.     if minError1 + minError2 < minError
27.       minError := minError1 + minError2
28.       aggregates := aggregates1  $\cup$  aggregates2
29.   }
30.   for  $i := 0$  to  $l - 1$  {
31.     [minError1, aggregates1] := COMPUTEMINERROR( $u$ ,  $x$ ,  $i$ )
32.     [minError2, aggregates2] := COMPUTEMINERROR( $v$ ,  $x$ ,  $k - i - 1$ )
33.     if minError1 + minError2 < minError
34.       minError := minError1 + minError2
35.       aggregates := aggregates1  $\cup$  aggregates2  $\cup \{x\}$ 
36.   }
37.   [subTree[ $x$ ,  $y$ ,  $l$ ].error, subTree[ $x$ ,  $y$ ,  $l$ ].aggregates] := [minError, aggregates]
38. }
39. subTree[ $x$ ,  $y$ ,  $l$ ].computed := true
40. return [subTree[ $x$ ,  $y$ ,  $l$ ].error, subTree[ $x$ ,  $y$ ,  $l$ ].aggregates]

```

FIGURE 3

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procedure COMBINEMINERROR()
1. for  $i = 1$  to  $m$ 
2.   for  $j = 0$  to  $k$  {
3.      $T_i[j].[\text{error}, \text{aggregates}] := \text{COMPUTEMINERROR}(r(T_i), \epsilon, j)$ 
4.      $X_i[j].[\text{error}, \text{aggregates}] := [\infty, \emptyset]$ 
5.   }
6.   for  $j = 0$  to  $k$ 
7.      $X_1[j].[\text{error}, \text{aggregates}] := T_1[j].[\text{error}, \text{aggregates}]$ 
8.   for  $i = 1$  to  $m$ 
9.     for  $j = 0$  to  $k$ 
10.      for  $l = 0$  to  $j$ 
11.        if  $(X_{i-1}[l].\text{error} + T_i[j-l].\text{error} < X_i[j].\text{error})$  {
12.           $X_i[j].\text{error} = X_{i-1}[l].\text{error} + T_i[j-l].\text{error}$ 
13.           $X_i[j].\text{aggregates} = X_{i-1}[l].\text{aggregates} \cup T_i[j-l].\text{aggregates}$ 
14.        }

```

FIGURE 4

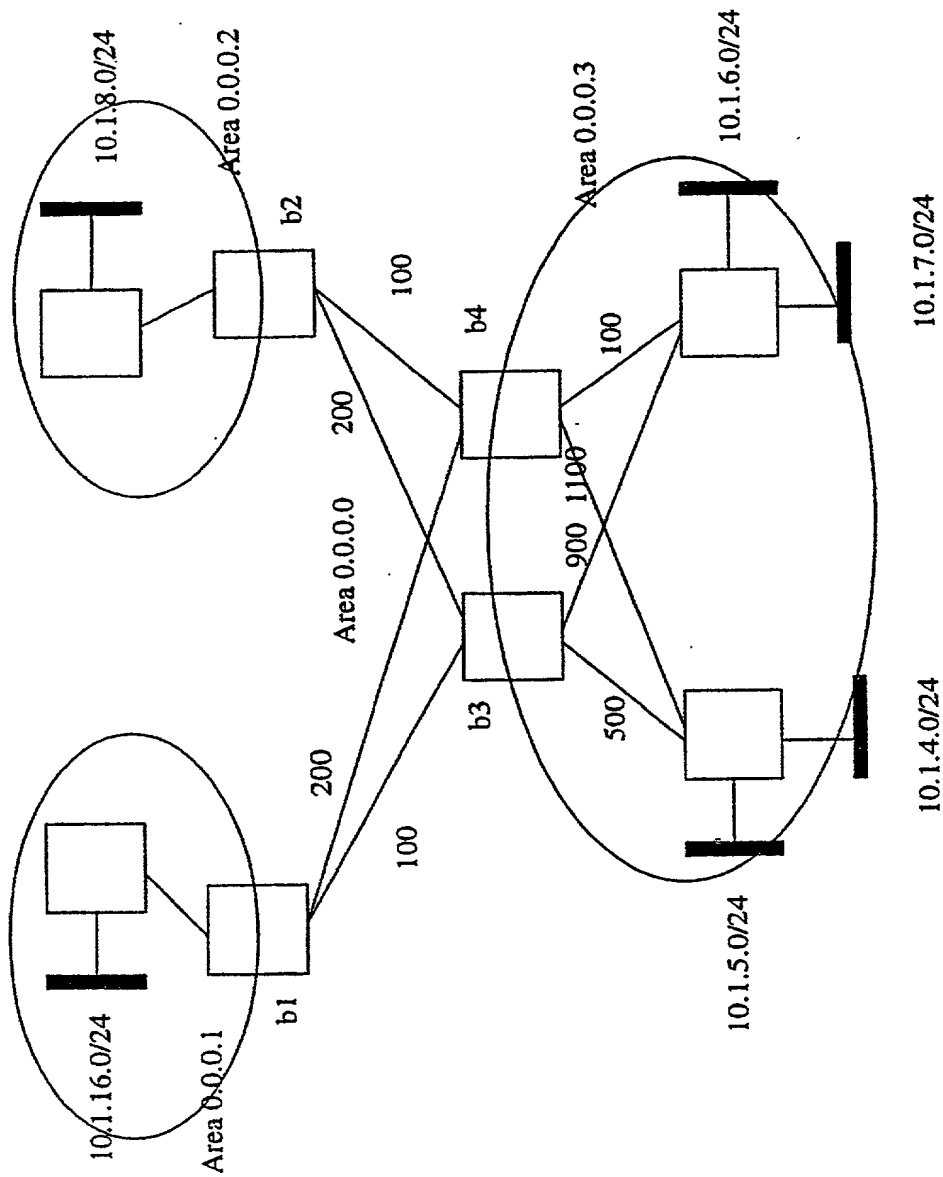


FIGURE 5

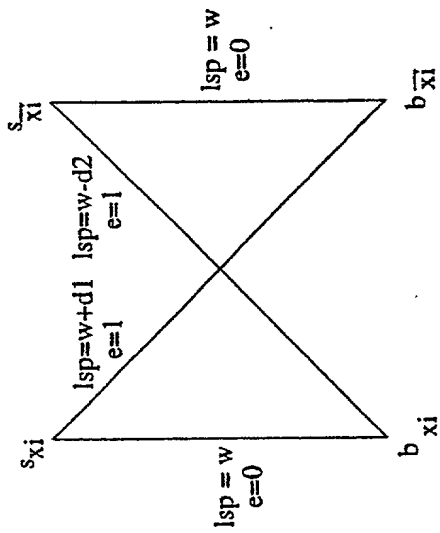
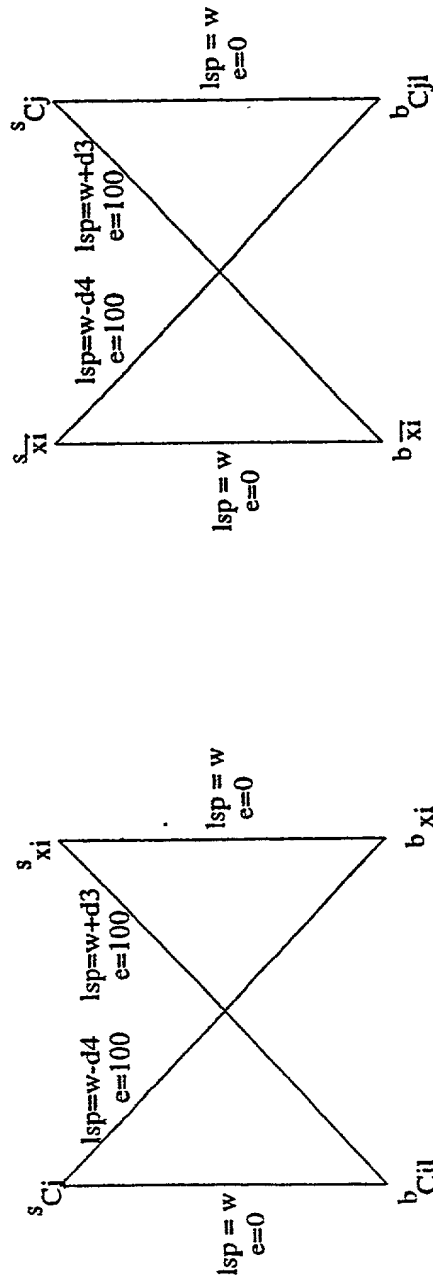


FIGURE 6



(a) $C_{ji} = x_i$

(b) $C_{ji} = \bar{x}_i$

FIGURE 7A

FIGURE 7B

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procedure COMPUTEWEIGHTSCUMULATIVE()
1. for each  $b \in B_i$  set  $W_{min}(b) := 0$ 
2. for  $i := 1$  to  $r$  {
3.    $W := W_{min}$ 
4.   Choose a random subset  $R \subseteq B_i$  of ABRs
5.   for each  $b \in R$  set  $W(b)$  to a random weight in  $[0, L]$ 
6.   if  $\sum_{s \in S} e(s, B(s, W)) < \sum_{s \in S} e(s, B(s, W_{min}))$ 
7.      $W_{min} := W$ 
8. }
9. return  $W_{min}$ 

```

FIGURE 8

procedure ComputeWeightsMax(Q)

1. for each $b \in B_i$ set Wold(b) := 0

2. while (Pb₂B

i Wold(b) ≤ (

j B_ij*(j B_ij-1)

2) *lspmax) f3. Let

Q0 be a new set of inequalities that result when the value Wold(b) is substituted for each variable W (b) only on the LHS of each inequality in Q 4. Set Wnew(b) to the smallest possible value such that each inequality in Q0 is satisfied when Wnew(b) is substituted for variable W (b) in Q0 5. if Wnew = Wold 6. return Wnew 7. else 8. Wold := Wnew 9. g 10. return "there does not exist a weight assignment W "

FIGURE 9

procedure COMPUTEWEIGHTSTWOABR()

1. Set $V_{opt} := v(s_1)$, $E := E_{opt} := \sum_{s \in S} e(s, b_1)$
2. for $j := 1$ to n {
3. $E := E + e(s_j, b_2) - e(s_j, b_1)$
4. if $E < E_{opt}$
5. $V_{opt} := v(s_{j+1})$, $E_{opt} := E$
6. }
7. return V_{opt}

FIGURE 10